

# **dMAzeRunner: Accelerating loop nests on dataflow accelerators**

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Joint work with:

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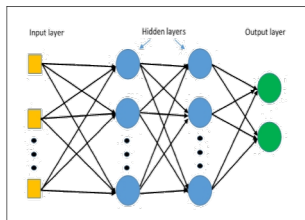
Sasikanth Avancha (Intel PCL)

Youngbin Kim and Kyoungwoo Lee (Yonsei)

# Must-Accelerate Applications in ML Era

## Widely Used ML Models

### Multi Layer Perceptrons



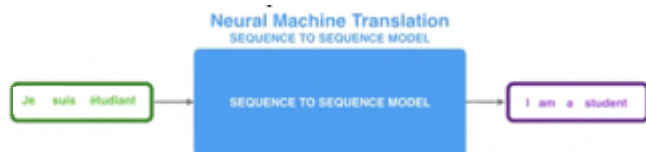
<http://yann.lecun.com/exdb/lenet/>

### Convolution Neural Networks



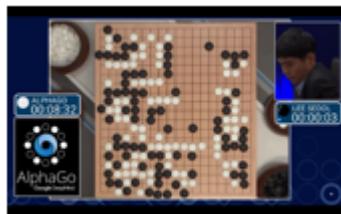
[http://vision03.csail.mit.edu/cnn\\_art/index.html](http://vision03.csail.mit.edu/cnn_art/index.html)  
<https://pjreddie.com/darknet/>

### Sequence Models



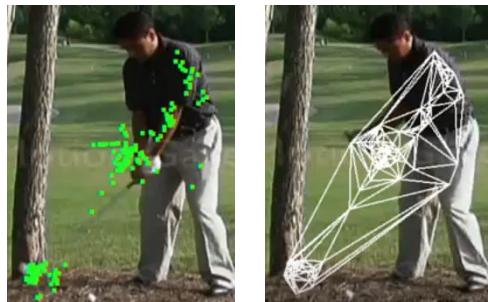
<http://jalamar.github.io/visualizing-neural-machine-translation-mechanics-of-seq2seq-models-with-attention/>  
<https://deeplearning.mit.edu/>

### Reinforcement Learning



AlphaGo.  
<https://www.nature.com/articles/nature24270>

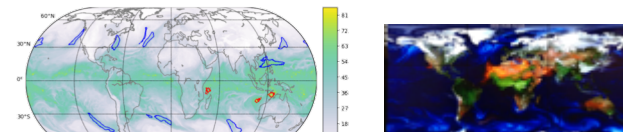
### Graph Neural Networks



Points of Interest      Delaunay Triangulation  
YOW! Data 2018 Conference.  
<https://www.youtube.com/watch?v=IDRb3CjESmM>

## Popular Applications

- ▶ **Object Classification/Detection**
- ▶ **Media Processing/Generation**
- ▶ **Large-Scale Scientific Computing**



<https://giphy.com>

Tropical Cyclon Detection

<https://insidehpc.com/2019/02/gordon-bell-prize-highlights-the-impact-of-ai/>

- ▶ **Designing Software 2.0**

Google shrinks language translation code from 500k LoC to 500

<https://jack-clark.net/2017/10/09/import-ai-63-google-shrinks-language-translation-code-from-500000-to-500-lines-with-ai-only-25-of-surveyed-people-believe-automation-better-jobs/>  
Kunle Olukotun, NeurIPS 2018 Invited talk.

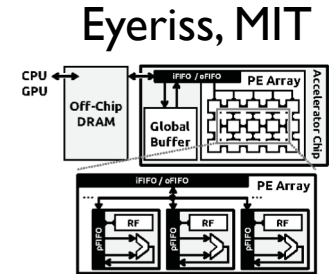
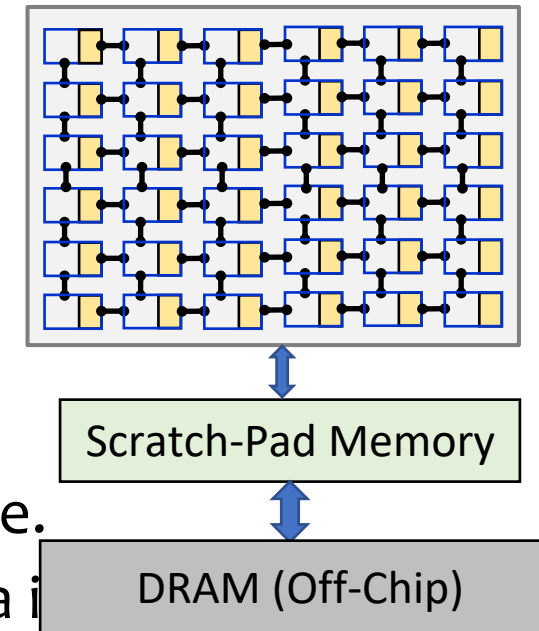
- ▶ **and more ...**

# Dataflow Accelerators: Promising Solution

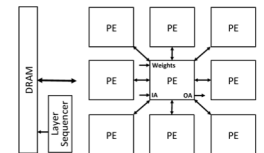
Known variations include - Systolic arrays,

- Spatially programmable architecture,
- Coarse-Grained Reconfigurable Arrays

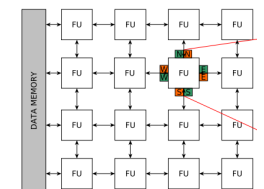
- ▶ Massive arrays of processing elements.
  - ▶ Simple: absence of complex OoO pipeline and decoding.
  - ▶ Programmable: accommodate executing all operations within loop.
- ▶ Private and shared memory for PEs sustain data reuse.
- ▶ PEs can be busy performing computations while data is being communicated from lower memories.
  - ▶ Taken care by effective data management i.e., software prefetching, data distribution, data allocation.



SCNN, nVIDIA

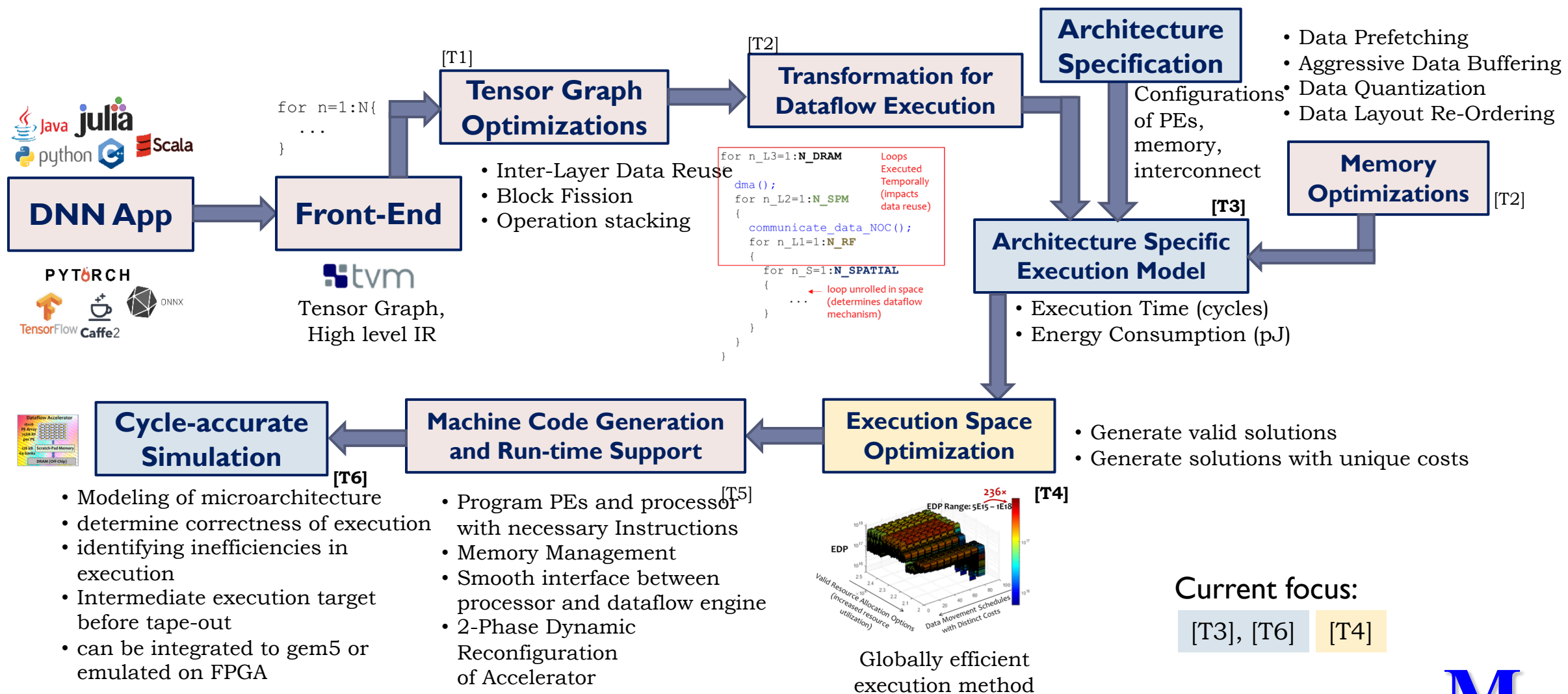


Hycube, NUS



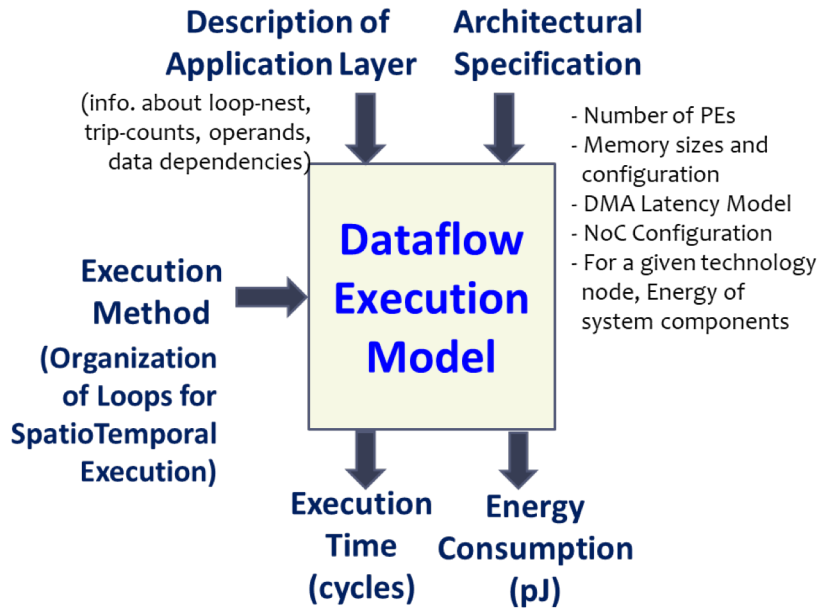
- [1] Norman Jouppi et al. In-datacenter performance analysis of a tensor processing unit. In ISCA 2017.
- [2] Yu-Hsin Chen et al. Eyeriss: An energy-efficient reconfigurable accelerator for deep cnns. In JSSC 2016
- [3] Dataflow Processing Unit from Wave Computing. In HOTCHIPS 2017.
- [4] M. Thottethodi and T. N. Vijaykumar. Why the GPGPU is Less Efficient than the TPU for DNNs. ACM SIGARCH Blog, Jan 2019. (online)
- [5] Bruce Fleischer et al., A Scalable Multi-TeraOPS Core for AI Training and Inference. In VLSI 2018.
- [6] Manupa Karunaratne et al. Hycube: A cgra with reconfigurable single-cycle multi-hop interconnect. In DAC 2017.

# Our current focus in the system stack





# Execution Modeling of Dataflow Accelerators



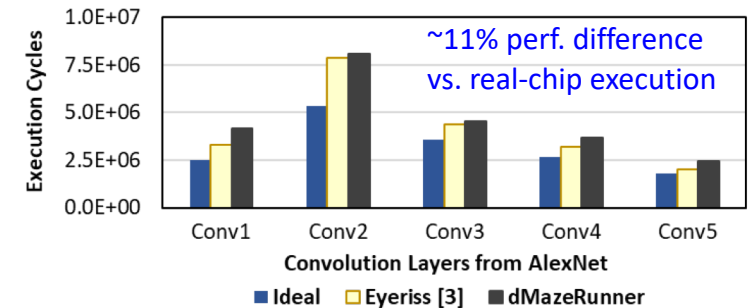
Features with detailed modeling of

- ✓ Analyze **arbitrary perfectly nested loops**.
- ✓ miss penalty and stall cycles (PE execution, managing PE/shared memory).
- ✓ **inter-PE communication**.
- ✓ **temporal/spatial data reuse**.
- ✓ Integrated **support common ML libraries** MXNet/Keras/Tensorflow/... (thanks TVM! – leveraging front-end)

Shail Dave, Youngbin Kim, Sasikanth Avancha, Kyoungwoo Lee, Aviral Shrivastava, dMazeRunner: Executing Perfectly Nested Loops on Dataflow Accelerators [CODES+ISSS, TECS 2019].

**Step-wise equations and analysis in the paper**

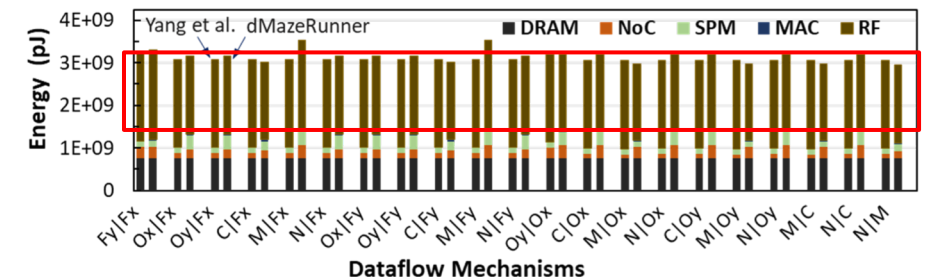
Validation of Dataflow Model against Eyeriss Chip



Chen, Yu-Hsin et al. "Eyeriss: An energy-efficient reconfigurable accelerator for deep convolutional neural networks." [JSSC '17]

Validation against DNN Optimizer of Yang et al.

Yang, Xuan, M. Gao, J. Pu, A. Nayak, Q. Liu, S. Bell, J. Setter, K. Cao, H. Ha, Christos Kozyrakis, and Mark Horowitz. "DNN Dataflow Choice Is Overrated." [arXiv '18]



- Energy estimate differs by ~4.2% for variety of execution methods
- For efficient mappings, major energy spent in RF accesses

# DiRAC: Microarch and Cycle-accurate Simulator

## Dynamically reconfigurable dataflow accelerator architecture template.

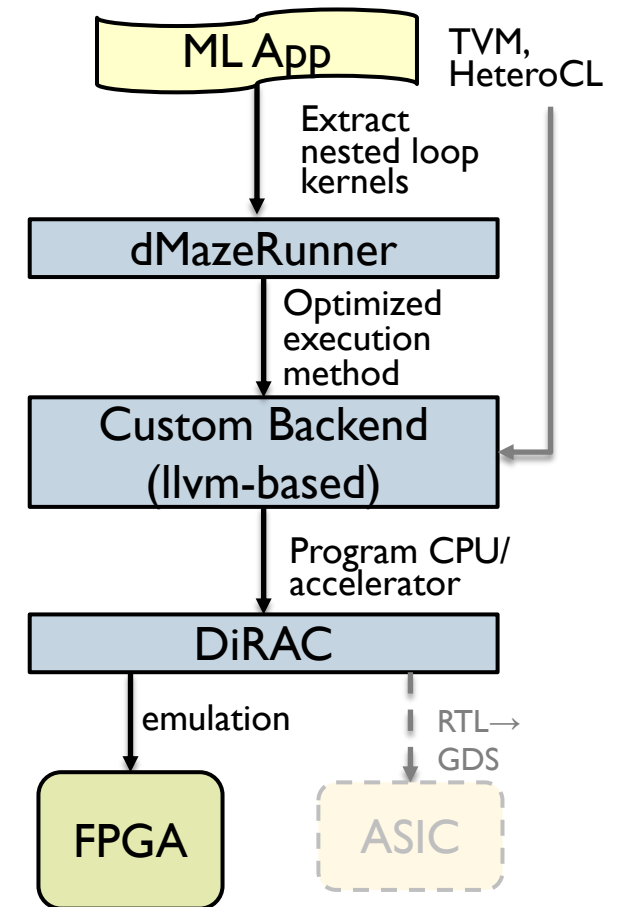
- ▶ (a)synchronous execution of pipelined PEs, double-buffered larger RFs
- ▶ Programmable multicast network for arbitrary dataflow
- ▶ 2D-mesh interconnect for fast inter-PE communications
- ▶ Multi-bank, conflict-free, software-directed scratchpad management
- ▶ Architectural template serves as a kick-starter baseline.  
Extend to support various interconnect/PEs/memory architecture

## Cycle-accurate simulation of accelerator system.

- ▶ Explore FSM/ISA variations for PEs and controller, sensitivity analysis,...
- ▶ Work-in-progress. Release planned in Q4 end (Dec '19).
- ▶ Next step: FPGA emulation for functional testing + rapid prototyping.
- ▶ Develop + Integrate area/power model for comprehensive design exploration.

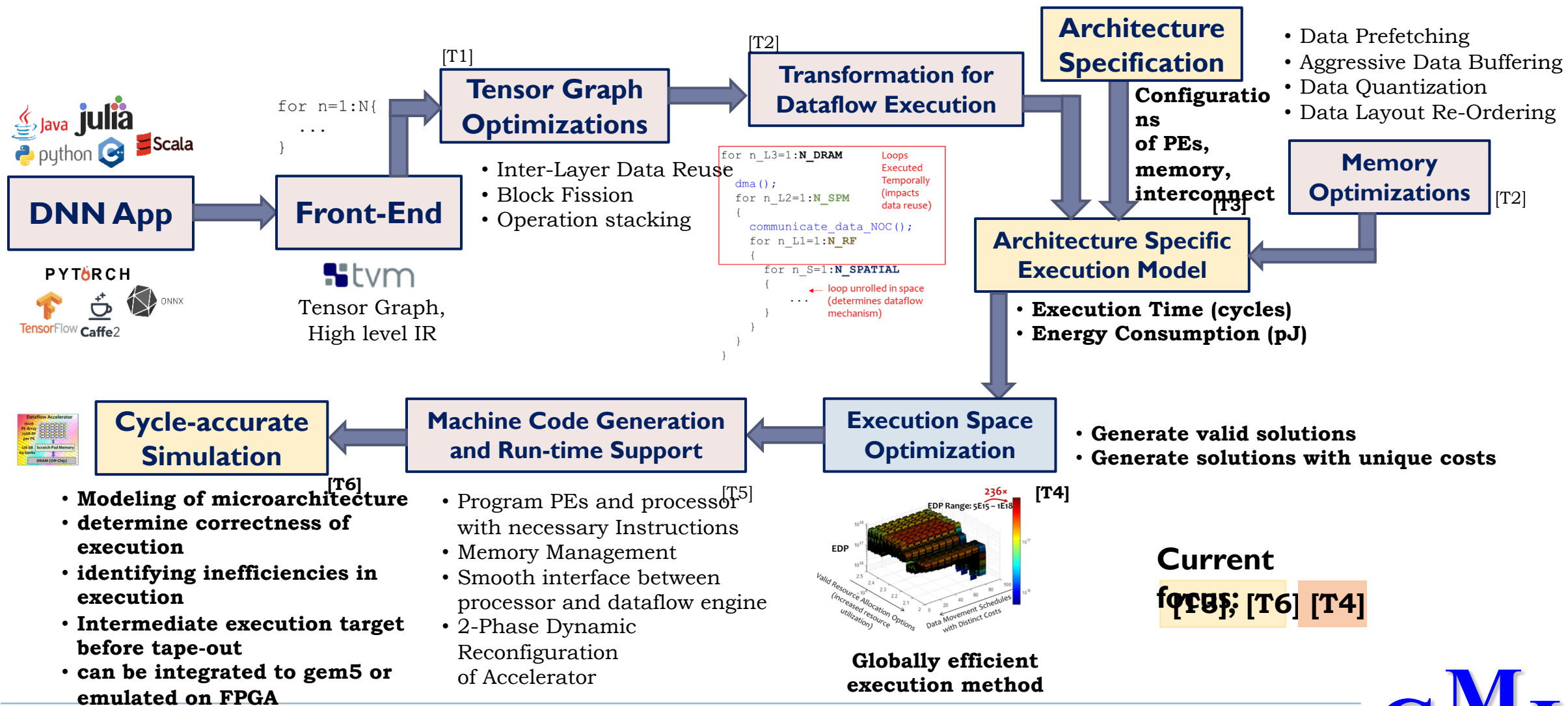
## Outcomes

- ▶ Validation of optimizations achieved through analytical modeling.
- ▶ Easy tool for prototyping domain-specific accelerator architecture.
- ▶ Educational/Training: Tool for teaching and hands-on with ML accelerators.



Plan for Integration of DiRAC with dMazeRunner.

# Our current focus in the system stack

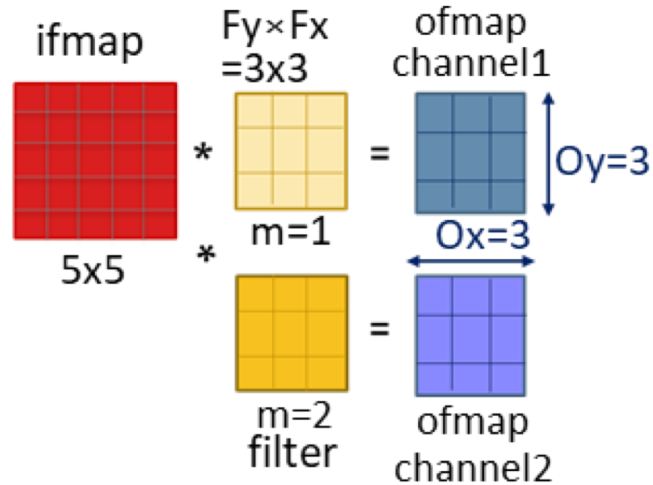


# Spatio-Temporal Execution on dataflow accelerators

```

for m=1:2
  for oy=1:3
    for ox=1:3
      for fy=1:3
        for fx=1:3
          O[m][oy][ox] +=
            I[oy+fy-1][ox+fx-1]
            * W[m][fy][fx];

```



```

% access DRAM once (no L3 loops)
dma() % prefetch data in 256B SPM

```

```

for m_L2=1:2
  for fy_L2=1:3

```

```

    access_SPM_and_comm_NoC();

```

```

    for fx_L1=1:3

```

data in RF is I: 1x3  
W: 1x1x3, O: 1x1x1

```

        for oy_S=1:3
          for ox_S=1:3

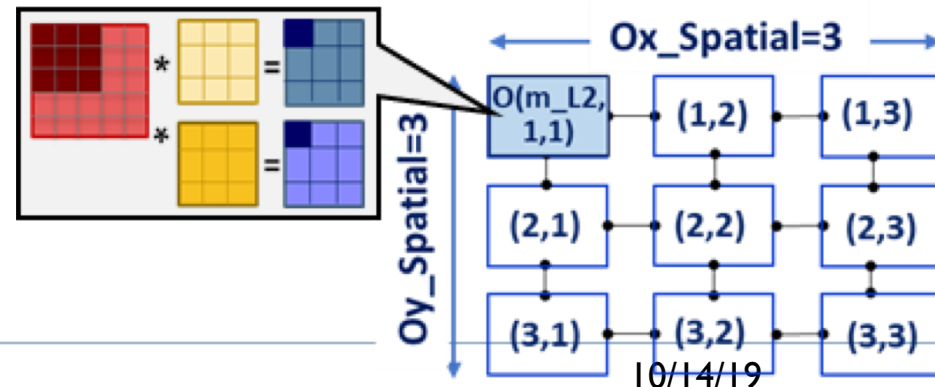
```

**Ofmaps  
Execute  
Spatially**

```

          O[m_L2][oy_S][ox_S] +=
            W[m_L2][fy_L2][fx_L1] *
            I[oy_S+fy_L2-1]
            [ox_S+fx_L1-1];

```



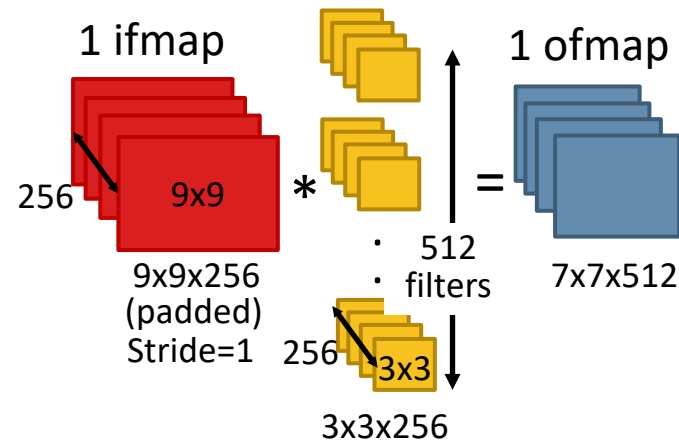
# Vast “Execution Method” Space

- ▶ Many many ways to execute nested loops (of DNN) on a dataflow accelerator
- ▶ Both software and hardware design space
- ▶ **Hardware:** Size, layout and connectivity of PEs, SPM size, no. of regs, NOC params, etc.
- ▶ **Software:** loop mappings, e.g.,  
**Spatial:** output stationary, or row stationary,  
**Temporal:** order and tiling of loops, data buffering, etc.

## 4D Convolution:

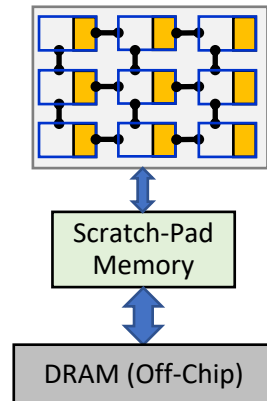
```
for n=1:N           % batch size
  for m=1:M           % filters
    for c=1:C          % channels
      for ox=1:Ox      % rows of ofmap
        for oy=1:Oy    % columns of ofmap
          for fx=1:Fx  % filter height
            for fy=1:Fy % filter width
              O[n][m][ox][oy] +=
                I[n][c][ox+fx-1][oy+fy-1] *
                W[m][c][fx][fy];
```

$\langle N, M, C, O_x, O_y, F_x, F_y \rangle =$   
 $\langle 1, 512, 256, 7, 7, 3, 3 \rangle$



Concurrent  
Execution  
on PEs  
in Space

## Accelerator



L1  
Accesses

L2  
Accesses

L3  
Accesses

Conv5\_2 [ResNet]



# Orchestration of Loops

## 4D Convolution:

```

for n=1:N           % batch size
  for m=1:M         % filters
    for c=1:C       % channels
      for ox=1:Ox   % rows of ofmap
        for oy=1:Oy % columns of ofmap
          for fx=1:Fx % filter height
            for fy=1:Fy % filter width
              O[n][m][ox][oy] +=
                I[n][c][ox+fx-1][oy+fy-1] *
                W[m][c][fx][fy];
            
```

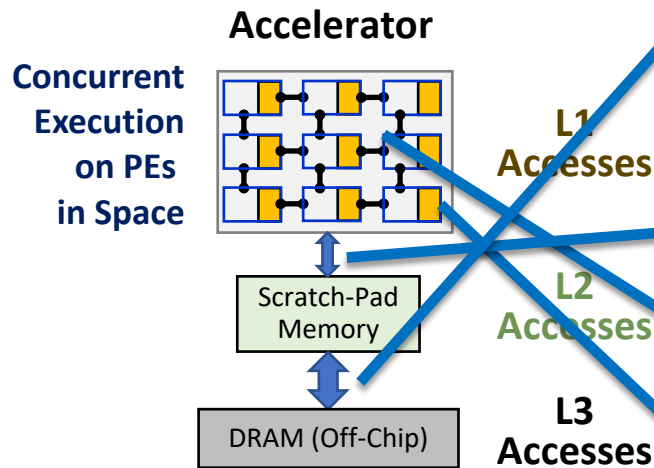
<N, M, C, Ox, Oy, Fx, Fy> =  
<8, 64, 32, 3, 3, 3, 3>

Ifmap: 8, 5x5x32

Filters: 64, 3x3x32

Ofmap: 8, 3x3x64

*All the tilings and re-orderings capture a vast space of "hardware-software execution methods" of the nested loops on the dataflow accelerator*



```

for n_L3 = 1:N_DRAM
  for m_L3 = 1:M_DRAM
    for c_L3 = 1:C_DRAM
      for ox_L3 = 1:Ox_DRAM
        for oy_L3 = 1:Oy_DRAM
          for fx_L3 = 1:Fx_DRAM
            for fy_L3 = 1:Fy_DRAM

```

```

{
  dma( );

```

```

    for n_L2 = 1:N_SPM
      for m_L2 = 1:M_SPM
        for c_L2 = 1:C_SPM
          for ox_L2 = 1:Ox_SPM
            for oy_L2 = 1:Oy_SPM
              for fx_L2 = 1:Fx_SPM
                for fy_L2 = 1:Fy_SPM

```

```

          {
            communicate_data_NoC( );

```

```

            for n_L1 = 1:N_RF
              for m_L1 = 1:M_RF
                for c_L1 = 1:C_RF
                  for ox_L1 = 1:Ox_RF
                    for oy_L1 = 1:Oy_RF
                      for fx_L1 = 1:Fx_RF
                        for fy_L1 = 1:Fy_RF

```

```

                      for n_S = 1:N_SPATIAL
                        for m_S = 1:M_SPATIAL
                          for c_S = 1:C_SPATIAL
                            for ox_S = 1:Ox_SPATIAL
                              for oy_S = 1:Oy_SPATIAL
                                for fx_L3 = 1:Fx_SPATIAL
                                  for fy_L3 = 1:Fy_SPATIAL
                                    O[][][][] +=
                                      I[][][][] *
                                      W[][][][];
                                
```

```

          }
        
```

```

      }
    
```

```

  }
}

```

# Config#1: 1D Spatial Execution

```
for m=1:2
  for ox=1:3
    for oy=1:3
      for fx=1:3
        for fy=1:3
```

```
      O[m][ox][oy] += W[m][fx][fy] ×
        I[ox+fx-1][oy+fy-1];
```



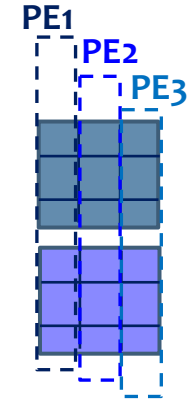
```
for m_T=1:2
  for fx_T=1:3
    for fy_T=1:3
      for ox_T=1:3
```

Remaining loops  
execute Temporally  
on every PEs

```
#pragma unroll spatial
for oy_S=1:3
```

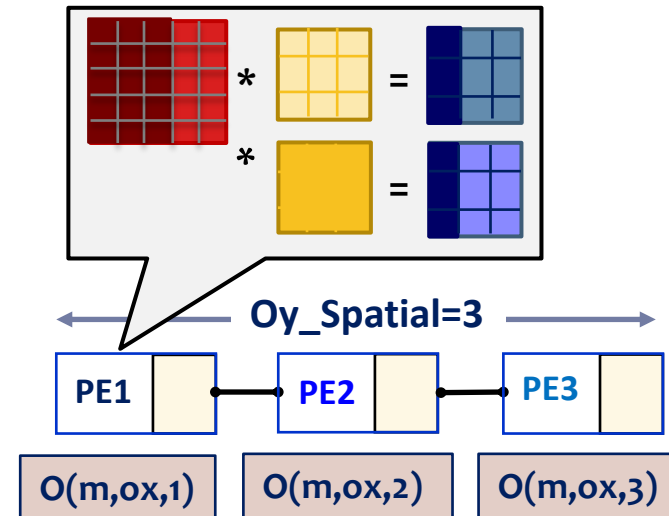
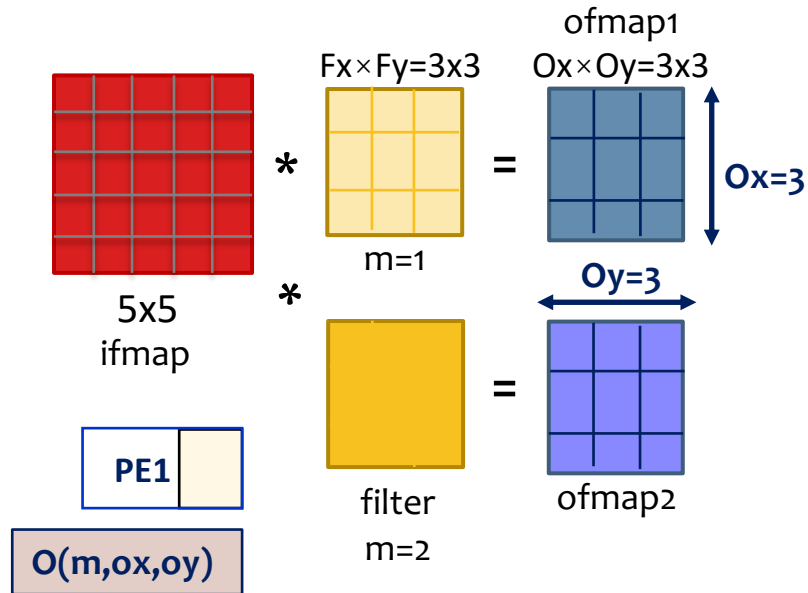
```
  O[m][ox][oy] += W[m][fx][fy] ×
    I[ox+fx-1][oy+fy-1];
```

Ofmap columns  
execute Spatially



execution on PE1

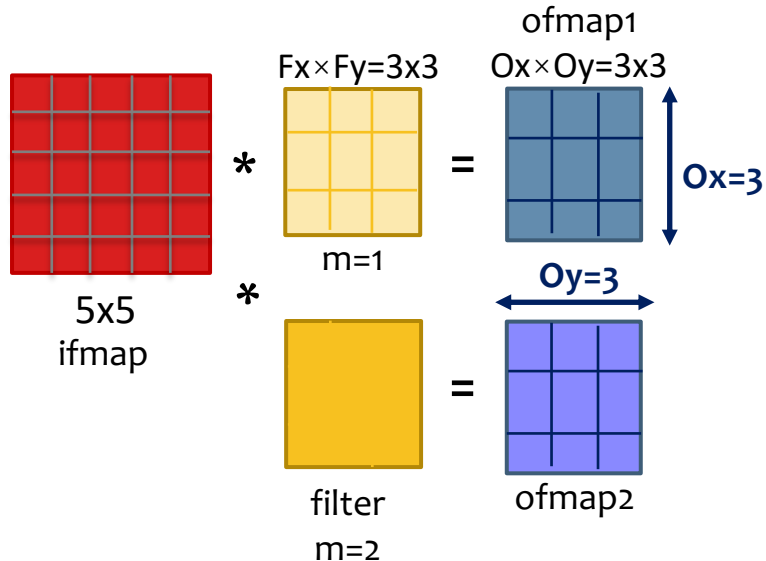
```
O[m_T][ox_T][1] +=
  W[m_T][fx_T][fy_T] ×
  I[ox_T+fx_T-1][fy_T]
```



# Config#2: 2D Spatial Execution

```
for m=1:2
  for ox=1:3
    for oy=1:3
      for fx=1:3
        for fy=1:3
```

```
      O[m][ox][oy] += W[m][fx][fy] ×
                    I[ox+fx-1][oy+fy-1];
```



```
    for m_T=1:2
      for fx_T=1:3
        for fy_T=1:3
```

**Loops for Filter Weights  
execute Temporally  
on every PEs**

```
    #pragma unroll spatial
```

```
    for ox_S=1:3
      for oy_S=1:3
```

**Ofmaps execute  
Spatially**

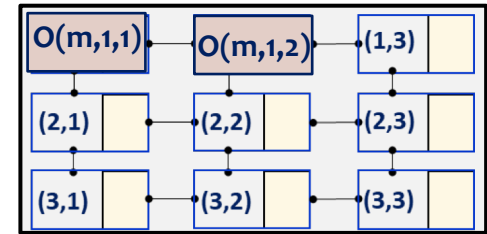
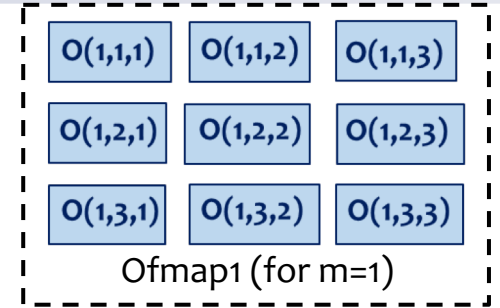
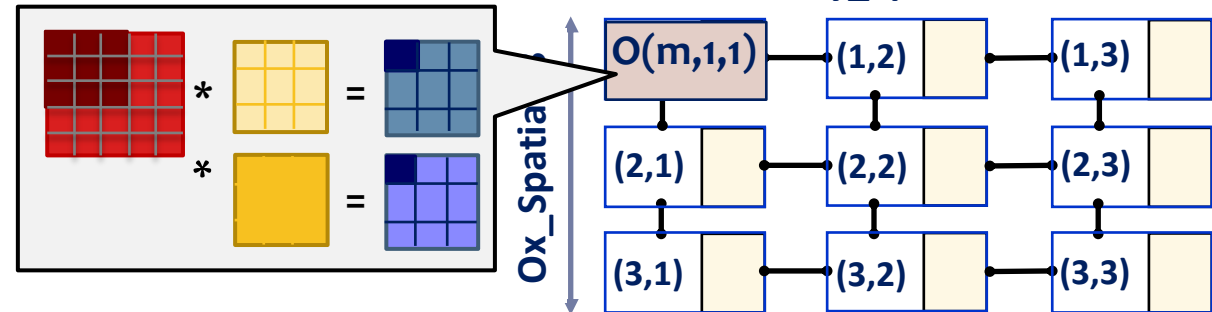
```
      O[m][ox][oy] += W[m][fx][fy] ×
                    I[ox+fx-1][oy+fy-1];
```

**execution on PE(1,1)**

$O[m_T][1][1] +=$

$W[m_T][fx_T][fy_T] \times$

$I[fx_T][fy_T]$



# Config#3: 3D Spatial Execution

```
for m=1:2
  for ox=1:3
    for oy=1:3
      for fx=1:3
        for fy=1:3
```

```
      O[m][ox][oy] += W[m][fx][fy] ×
        I[ox+fx-1][oy+fy-1];
```

```
for fx_T=1:3
  for fy_T=1:3
```

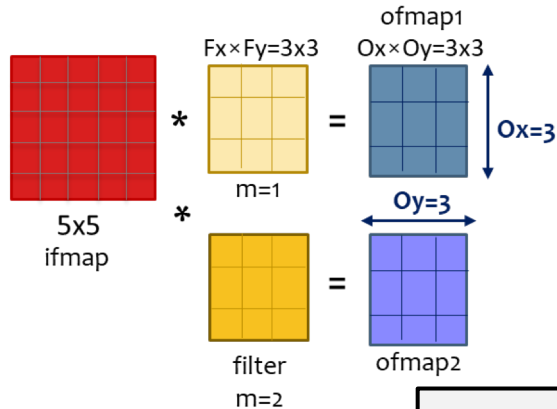
**Loops for weights execute  
Temporally on every PEs**

```
#pragma unroll spatial
```

```
for m_S = 1:2
  for ox_S=1:3
    for oy_S=1:3
```

**Entire ofmap  
execute Spatially**

```
      O[m][ox][oy] += W[m][fx][fy] ×
        I[ox+fx-1][oy+fy-1];
```

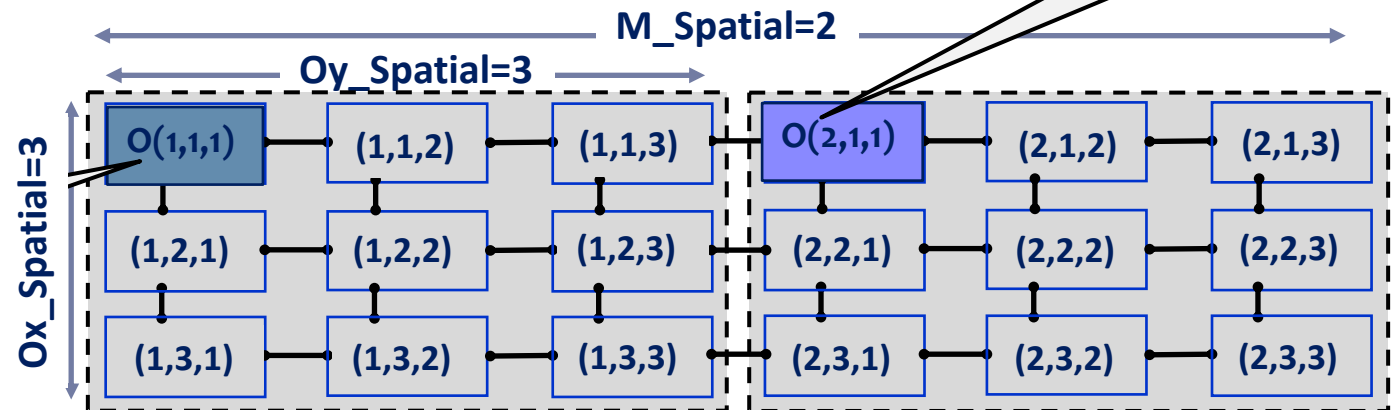
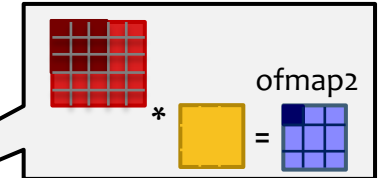


**execution on PE(1,1,1)**

$O[1][1][1] += W[1][fx\_T][fy\_T] \times I[fx\_T][fy\_T]$

**execution on PE(2,1,1)**

$O[2][1][1] += W[2][fx\_T][fy\_T] \times I[fx\_T][fy\_T]$



# Reordering of the loops → Different dataflow

```

for m=1:2
  for ox=1:3
    for oy=1:3
      for fx=1:3
        for fy=1:3
          O[m][ox][oy] +=
            W[m][fx][fy] ×
            I[ox+fx-1][oy+fy-1];

```

→

```

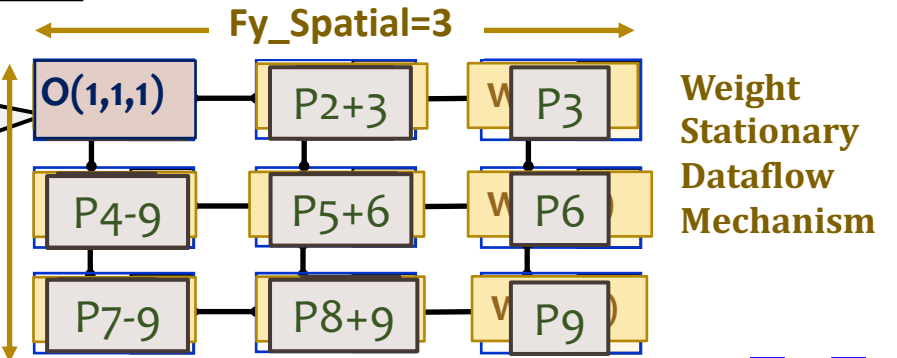
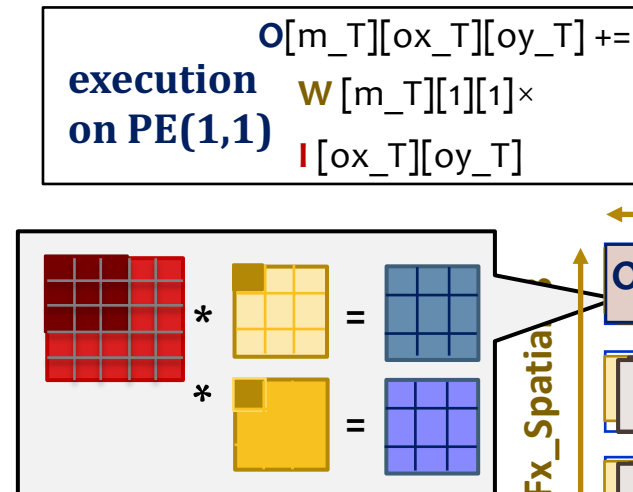
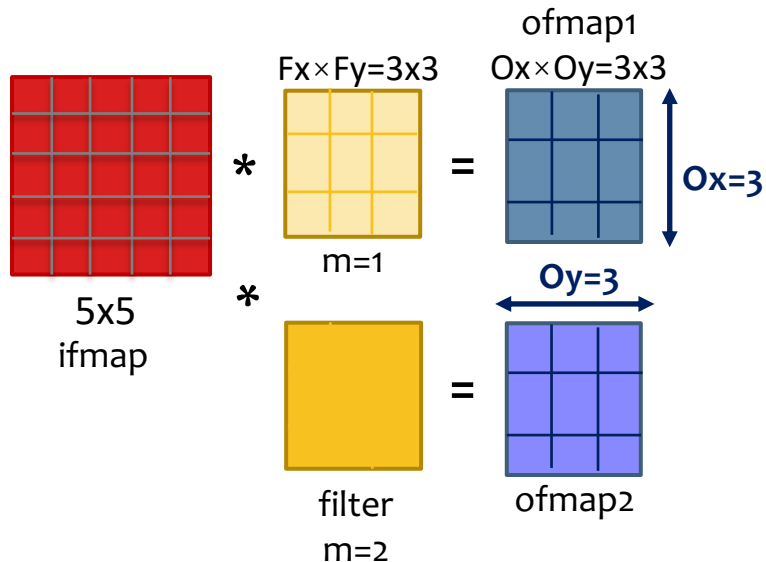
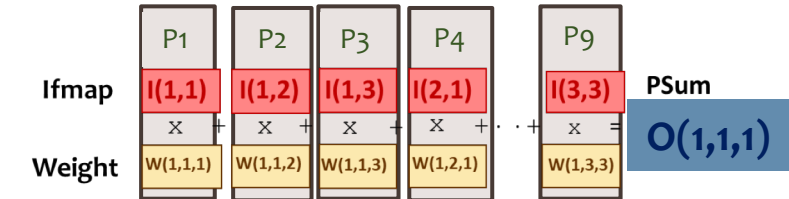
for m_T=1:2
  for ox_T=1:3
    for oy_T=1:3
      #pragma unroll spatial
      for fx_S=1:3
        for fy_S=1:3
          O[m][ox][oy] +=
            W[m][fx][fy] ×
            I[ox+fx-1][oy+fy-1];

```

**Loops for Filter Weights execute Temporally on every PEs**

**Weights laid out Spatially**

Unrolling some other two loops spatially





# Exploration of “execution methods”

## 4D Convolution:

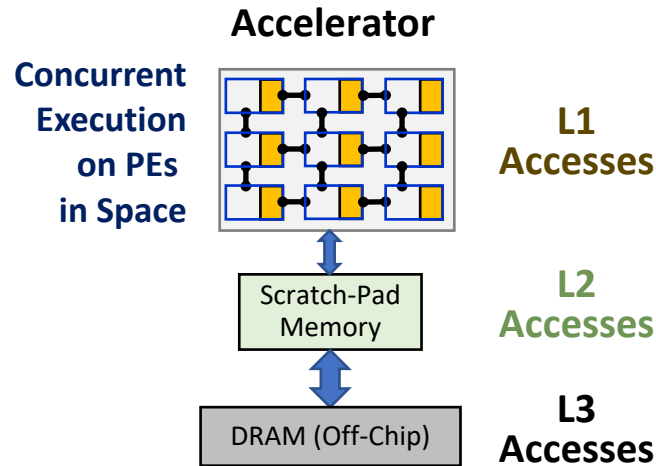
```

for n=1:N           % batch size
  for m=1:M         % filters
    for c=1:C       % channels
      for ox=1:Ox   % rows of ofmap
        for oy=1:Oy % columns of ofmap
          for fx=1:Fx % filter height
            for fy=1:Fy % filter width
              O[n][m][ox][oy] +=
                I[n][c][ox+fx-1][oy+fy-1] *
                W[m][c][fx][fy];
            
```

<N, M, C, Ox, Oy, Fx, Fy> =  
 <8, 64, 32, 3, 3, 3, 3>

**Ifmap:** 8, 5x5x32  
**Filters:** 64, 3x3x32  
**Ofmap:** 8, 3x3x64

*The problem of exploring the  
 “execution methods” becomes the  
 problem of exploring all the  
 possibilities of tiling and ordering  
 factors in the 28-dimensional loop*



```

for n_L3 = 1:N_DRAM
  for m_L3 = 1:M_DRAM
    for c_L3 = 1:C_DRAM
      for ox_L3 = 1:Ox_DRAM
        for oy_L3 = 1:Oy_DRAM
          for fx_L3 = 1:Fx_DRAM
            for fy_L3 = 1:Fy_DRAM
              {
                dma( );
                for n_L2 = 1:N_SPM
                  for m_L2 = 1:M_SPM
                    for c_L2 = 1:C_SPM
                      for ox_L2 = 1:Ox_SPM
                        for oy_L2 = 1:Oy_SPM
                          for fx_L2 = 1:Fx_SPM
                            for fy_L2 = 1:Fy_SPM
                              {
                                communicate_data_NoC( );
                                for n_L1 = 1:N_RF
                                  for m_L1 = 1:M_RF
                                    for c_L1 = 1:C_RF
                                      for ox_L1 = 1:Ox_RF
                                        for oy_L1 = 1:Oy_RF
                                          for fx_L1 = 1:Fx_RF
                                            for fy_L1 = 1:Fy_RF
                                              {
                                                for n_S = 1:N_SPATIAL
                                                  for m_S = 1:M_SPATIAL
                                                    for c_S = 1:C_SPATIAL
                                                      for ox_S = 1:Ox_SPATIAL
                                                        for oy_S = 1:Oy_SPATIAL
                                                          for fx_L3 = 1:Fx_SPATIAL
                                                            for fy_L3 = 1:Fy_SPATIAL
                                                              {
                                                                O[][][][] +=
                                                                  I[][][][] *
                                                                  W[][][][];
                                                              }
                                                            }
                                                          }
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}

```

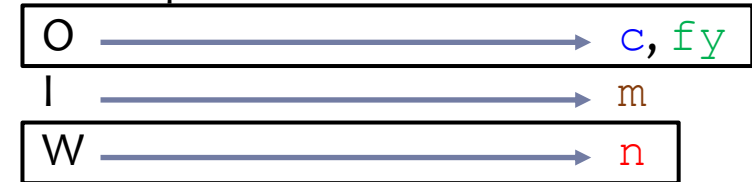
# Drastic pruning of Search Space

## Example: Generating loop-orderings with unique data reuse factors

```

for n = 1:N=2
  for m = 1:M=8
    for c = 1:C=4
      for fy = 1:Fy=3
        O[n][m] += I[n][c][fy] * W[m][c][fy]
      
```

is invariant across  
loops with index variables



**5 schedules with unique reuse costs  
as compared to  $4! = 24$  schedules**

Loop with index  
variable 'n' is  
innermost

Schedule	I	W	O
$\{\dots, n\}$	-	$N = 2$	-
$\{\dots, m\}$	$M = 8$	-	-
$\{\dots, m, c\}$	-	-	$C = 4$
$\{\dots, m, fy\}$	-	-	$Fy = 3$
$\{\dots, m, fy, c\}$	-	-	$C * Fy = 4 * 3$

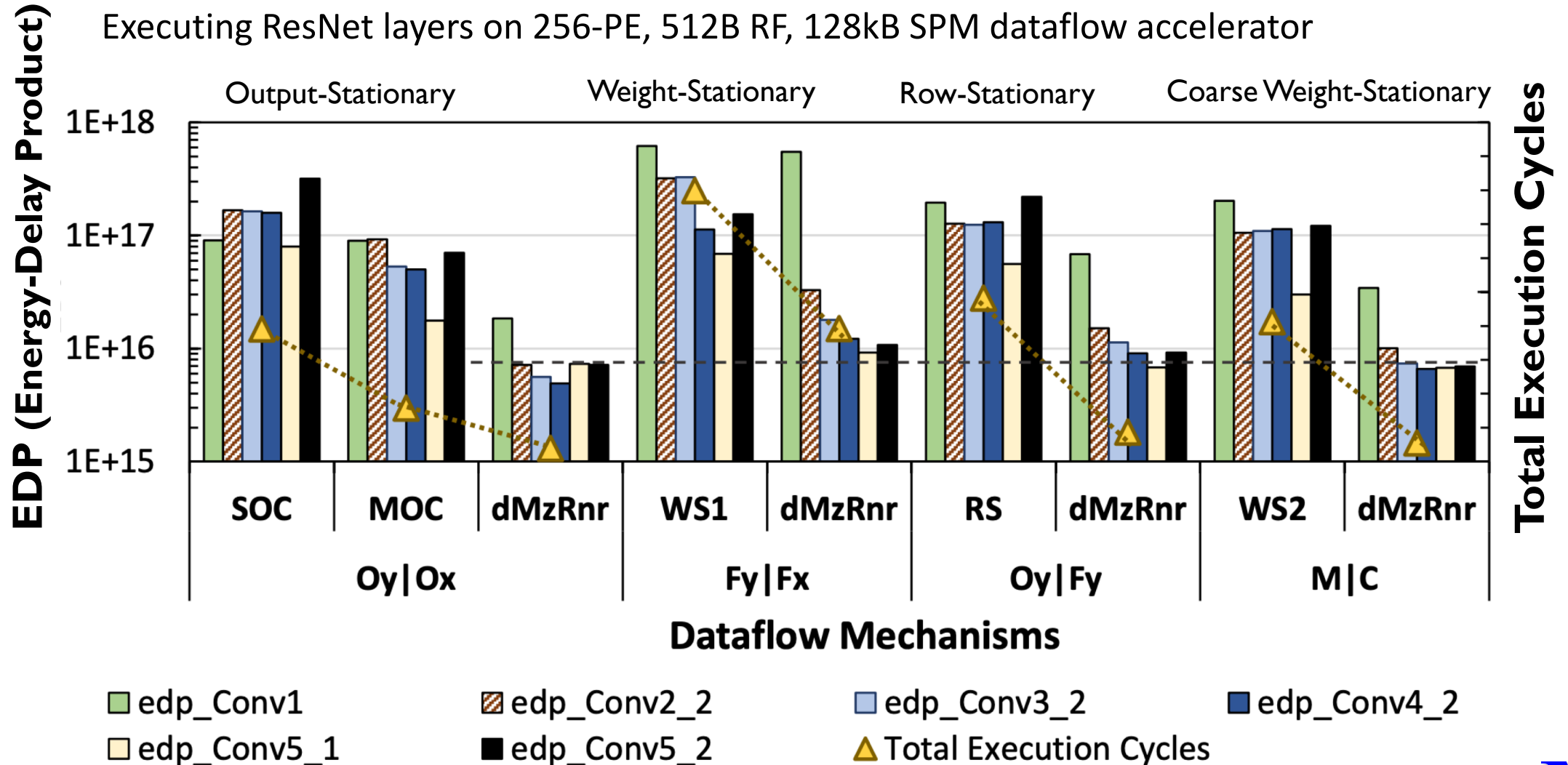
Reuse Factor for Data Operands

Interpretation:

$2 * 8 * 4 * 3$  accesses total  
W is loaded only  $8 * 4 * 3$  times

Operand 'O' is  
reused across  
both loops

# Results: 9X reduction in EDP



# Adaptable Mappings Yield Better Results

- ▶ Adapts to kernel/arch characteristics
  - ▶ Scales for layers/tensors of different shapes
- ▶ Finds non-intuitive mappings that optimizes various factors e.g.,
  - ✓ High resource utilization
  - ✓ Maximized reuse of multiple data operands
  - ✓ Minimized DRAM accesses
  - ✓ Efficient interleaving of computation with communication latency

Example Mappings of ResNet Conv5\_2 for Output-Stationary Dataflow

	MOC							dMazeRunner						
Tiling Factors	N	M	C	Ox	Oy	Fx	Fy	N	M	C	Ox	Oy	Fx	Fy
SPATIAL	1	4	1	7	7	1	1	1	4	1	7	7	1	1
RF	1	2	8	1	1	3	3	4	16	1	1	1	3	3
SPM	2	2	8	1	1	1	1	1	1	8	1	1	1	1
DRAM	2	32	8	1	1	1	1	1	8	64	1	1	1	1
Base	4	512	512	7	7	3	3	4	512	512	7	7	3	3
L2_Order	{n_L2, m_L2, oy_L2, ox_L2, fy_L2, fx_L2, c_L2} (outer to inner)							{n_L2, m_L2, oy_L2, ox_L2, fy_L2, fx_L2, c_L2} (outer to inner)						
L3_Order	{n_L3, m_L3, oy_L3, ox_L3, fy_L3, fx_L3, c_L3} (outer to inner)							{n_L3, m_L3, oy_L3, ox_L3, fy_L3, fx_L3, c_L3} (outer to inner)						

MOC: Simultaneous spatial processing of Multiple Output Channels [1, 2]

	For data allocated in RFs of PEs,	MOC	dMzRnr
PE Compute vs. Data comm. Latency:	144 vs. 648	576 vs. 576	
Total cycles:	~10,616,832	~2,459,648	
Ideal execution cycles for output-stationary:	2,359,296	2,359,296	
Reduction in DRAM accesses (ifmaps, weights):	(1x, 1x)	(4.57x, 2x)	
Perf. improvement (normalized to MOC):	1x	4.44x	
Energy-Delay-Product reduction (normalized):	1x	9.86x	

[1] S. Gupta et al. Deep learning with limited numerical precision. In ICML, 2015.

[2] Y. Chen et al. Eyeriss: A spatial architecture for energy-efficient dataflow for CNNs. In ISCA 2016.

# Achieving Close-to-Optimal Solutions in Seconds

- ▶ **Even domain non-experts can explore the space**

```
python run_optimizer.py --frontend mxnet  
                        --model resnet18 --layer-index 0
```

- ▶ **Does not preclude experts/programmers** from directing the search.

- ▶ In-built support for a few common opt strategies.

- ▶ **Quick exploration:**

- ▶ EDP ~2% higher vs. optimal of brute-force search (**seconds vs. days/hours**)
  - ▶ Implementation – **multi-threaded, caches commonly invoked routines** of analytical model.
  - ▶ Enables effective DSE of architecture.

[Alpha Release] <https://github.com/cmlasu/dMazeRunner>

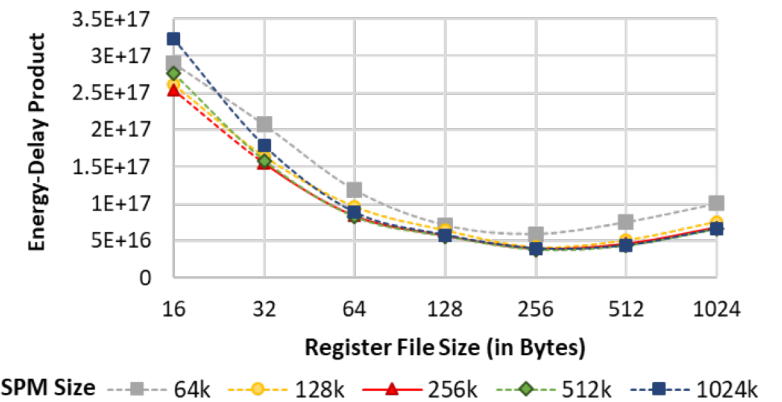
Search Space Exploration on  
an Intel i7-6700 Quad-core CPU

**min: 1 second**, ResNet conv5\_2  
(753 methods)

**max: 122 seconds**, ResNet conv2\_2  
(122092 methods)

[dMazeRunner, CODES+ISSS '19]

Optimizing Memory Sizes for ResNet18 Layers  
DSE for 256-PE CGRA



```
python tune_memory.py run <layer_index>
```



# Summary and Next Steps

- ▶ Coarse-grained dataflow accelerators promising for accelerating ML models.
  - ▶ Challenge: Programming the accelerators
  - ▶ System stack can extend the applicability.
- ▶ dMazeRunner App Mapping Framework
  - ▶ Analytical Power and performance model
  - ▶ Automated Design Space Exploration
- ▶ End-to-end system [WIP]
  - ▶ Programmable Microarch + Simulator
  - ▶ FPGA emulation
- ▶ Further Opportunities
  - ▶ Sparsity [WIP]: Support dynamic sparsity of varying levels (inference + training).
  - ▶ Multi-chip module accelerations
- ▶ Exciting times ahead!

 TensorFlow



TVM (UW)

  **dMazeRunner**  
**Libraries for accelerator execution**

  **DiRAC**

Chisel Vivado

Application
Algorithm
Programming Language
Libraries/Utilities
Compiler
Operating (Runtime) System
Instruction Set Architecture
Microarchitecture
Logic (Register-Transfer Level)
Circuits
Devices/Technology